



QP CODE: 21000689

Reg No :

Name :

M Sc DEGREE (CSS) EXAMINATION, JULY 2021

Fourth Semester

Faculty of Science

Elective - ME800402 - ALGORITHMIC GRAPH THEORY

M Sc MATHEMATICS, M Sc MATHEMATICS (SF)
2019 Admission Onwards

0B9047E8

Time: 3 Hours

Weightage: 30

Part A (Short Answer Questions)

Answer any **eight** questions.

Weight 1 each.

- 1. Construct a graph of order 5 whose vertices have degrees 1, 2, 2, 3, 4. What is the size of this graph?
- 2. Write an algorithm to determine the first word alphabetically from a list of n words, and output this word and its location in the list.
- 3. What is adjacency matrix of a graph? Draw the graph G be with vertex set $V(G) = \{v_1, v_2, v_3, v_4, v_5, v_6\} \ , E(D) = \{v_1v_2, v_1v_3, v_2v_3, v_3v_4, v_3v_5\}.$ Find adjacency matrix of G.
- 4. Define a forest. Give an example.
- 5. State Cayley's Tree formula.
- 6. Define distance function on a graph G. Show that it is a metric.
- 7. Define vertex connectivity of a graph. Find $\kappa(K_{m,n})$
- 8. Define an edge disjoint u-v path in a graph G and the term $\lambda(u,v)$, where $u,v\in V(G)$
- 9. Define a feasible vertex labeling of a weighted complete bipartite graph
- 10. Define a $\{b, v, r, k, \lambda\}$ design and state Fisher's inequality

(8×1=8 weightage)



Part B (Short Essay/Problems)

Answer any **six** questions.

Weight **2** each.

- 11. Define (a) a non-separable graph, (b) a block, (c) an end-block in a graph. Give examples for each.
- 12. (a) Explain indegree, outdegree and degree of a vertex in a digraph. Draw a digraph and find indegree, outdegree and degree of each vertex.
 - (b) State and prove The First Theorem on Digraph Theorey.
- 13. If T is a balanced complete binary tree of height h and order p, then prove that $h = \lceil log_2(\frac{p+1}{2}) \rceil$
- 14. Explain BFS Algorithm
- 15. Define a flow in a network N. Give an example of a flow where flow along each arc is a positive integer.
- 16. In a network, show that the value of a maximum flow equals the capacity of a minimum cut.
- 17. Let G be a bipartite graph with partite sets V_1 and V_2 . Prove that the set V_1 can be matched to a subset of V_2 if and only if V_1 is non deficient
- 18. Prove that every bridgeless cubic graph contains a 1-factor

(6×2=12 weightage)

Part C (Essay Type Questions)

Answer any **two** questions.

Weight **5** each.

- 19. a) An edge e of a connected graph is a bridge if and only if e does not lie on any of the cycle on G. b) Show that every u v walk in a graph contains a u v path.
- 20. Write an algorithm to determine a critical path in an activity digraph D with start vertex S and terminal vertex T.
- 21. State and prove a necessary and sufficient condition that a flow f in a network N with underlying digraph D is a maximum flow.
- 22. State and prove Berge's theorem to determine the maximum matching in a graph G.

(2×5=10 weightage)