



QP CODE: 22103101	Reg No	:	***************************************
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B.Sc DEGREE (CBCS) REGULAR / IMPROVEMENT / REAPPEARANCE EXAMINATIONS, OCTOBER 2022

Second Semester

Complementary Course - MM2CMT01 - MATHEMATICS - INTEGRAL CALCULUS AND DIFFERENTIAL EQUATIONS

(Common for B.Sc Chemistry Model I, B.Sc Chemistry Model II Industrial Chemistry, B.Sc Chemistry Model III Petrochemicals, B.Sc Electronics and Computer Maintenance Model III, B.Sc Food Science & Quality Control Model III, B.Sc Geology Model I, B.Sc Geology and Water Management Model III, B.Sc Physics Model I, B.Sc Physics Model II Applied Electronics, B.Sc Physics Model II Computer Applications, B.Sc Physics Model III Electronic Equipment Maintenance)

2017 ADMISSION ONWARDS

F6763D20

Time: 3 Hours

Max. Marks: 80

Part A

Answer any ten questions.

Each question carries 2 marks.

- 1. The solid lies between the planes perpendicular to the x-axis at x = 0 and x = 4. The cross-sections perpendicular to the axis on the interval $0 \le x \le 4$ are squares whose diagonals run from the parabola $y = -\sqrt{x}$ to the parabola $y = \sqrt{x}$. Find the volume of the solid.
- 2. Find the volume of the solid generated by revolving the region bounded by the curve $y = x^2$ and the lines y = 0, x = 2 about the x-axis.
- 3. The region in the first quadrant enclosed by the parabola $y = x^2$, the y-axis and the line y = 1 is revolved about the line $x = \frac{3}{2}$ to generate a solid. Find the volume of the solid.
- 4. Evaluate the double integral $\iint_R y^2 x \, dA$ over the rectangle $R=\{(x,y): -3 \leq x \leq 2, 0 \leq y \leq 1\}$.
- 5. Use a double integral to find the volume of the solid that is bounded above by the plane z=4-x-y and below by the rectangle $R=[0,1]\times[0,2]$.



- 6. Use a double integral to find the area of the region enclosed between the parabola $y=rac{1}{2}x^2$ and the line y=2x.
- 7. Verify that the function $x^2+y^2=c$ is a solution of the differential equation $y\frac{dy}{dx}+x=0.$
- 8. Examine whether the differential equation $(x^2-y^2)dx+(x^2-2xy)dy=0$ is exact or not.
- 9. Solve the differential equation xdy ydx = 0.
- 10. Write the general form of the integral curves of the set of equations $\frac{dx}{P}=\frac{dy}{Q}=\frac{dz}{R}$.
- 11. Define partial differential equations with examples
- 12. Find the general integral of the linear partial differential equation xp+yq=z (10×2=20)

Part B

Answer any six questions.

Each question carries 5 marks.

- 13. Find the length of the curve $y = (\frac{x}{2})^{\frac{2}{3}}$, from x = 0 to x = 2.
- 14. Find the area of the surface generated by revolving the curve $x=\frac{y^4}{4}+\frac{1}{8y^2}$, $0 \le y \le 2$, about the x-axis.
- 15. Find the average value of $f(x,y)=\sin{(x+y)}$ over the rectangle $0\leq x\leq \pi,\ 0\leq y\leq \pi.$
- 16. Use a triple integral to find the volume of the solid within the cylinder $x^2+y^2=9$ and between the planes z=1 and x+z=5.
- 17. Find values of A and B so that the function y(x) = Asinx + Bcosx + 1 satisfy the initial conditions $y(\pi) = 0, y'(\pi) = 0$.
- 18. Solve ylogydx + (x logy)dy = 0.
- 19. Solve $x rac{dy}{dx} + y = y^2 log x$
- Find the integral curves of the equations $\dfrac{dx}{z^2-2yz-y^2}=\dfrac{dy}{xy+zx}=\dfrac{dz}{xy-zx}$.



21. Form the partial differential equation by eliminating the arbitrary constants from $z=ax+by+\sqrt{a^2+b^2}$

 $(6 \times 5 = 30)$

Part C

Answer any two questions.

Each question carries 15 marks.

- 22. (a) The region bounded by the curve $y=\sqrt{4x-x^2}$, the x-axis and the line x = 2 is revolved about x-axis to generate a solid. Find the volume of the solid.
 - (b) Find the volume of the solid generated by revolving the region bounded by the curve $y=\sqrt{x}$, the x-axis and the line x = 4 about (i) x-axis (ii) y-axis.
- 23. (i) Evaluate $\int_{0}^{1} \int_{\frac{y}{2}}^{1} e^{x^{2}} dx dy$.
 - (ii) Change the order of integration and hence evaluate the double integral $\int_0^1 \int_x^{2-x} \frac{x}{y} \ dy dx$.
- 24. a) Solve $x^2(y+1)dx+y^2(x-1)dy=0$. b) Solve $4xdy-ydx=x^2dy$.
- 25. Show that the condition that the surfaces $F(x,y,z)=0,\ G(x,y,z)=0$ should touch is that the eliminant of x,y and z from these equations and the equations

$$rac{F_x}{G_x}=rac{F_y}{G_y}=rac{F_z}{G_z}$$
 should hold. Hence find the condition that the plane $lx+my+nz+p=0$ should touch the central conicoid $ax^2+by^2+cz^2=1$. (2×15=30)